

# A statistical approach to speaker identification in forensic phonetics field

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**Abstract.** Speaker identification can be summarized as the classification task that determines if two voices were spoken by the same person or not. It is a thoroughly studied topic, since it has applications in many fields. One is forensic phonetics, considered very hard since the expert has to face ambient noise, very short recordings, interference, loss of signal, and so on. For decades, these problems have been tackled by experts using their listening abilities, and each of them might represent a research area on its own. The use of automatic techniques may represent a modern alternative to the subjective evaluation of experts, that may enforce fairness of the classification procedure. In a nutshell, we use the differences in speech of a set of different voices to build a population model, and the suspected person’s voice to build a speaker model. The classification is carried out evaluating the similarity of a further speech sample with respect to the models. Preliminary evaluations shown that our approach reaches promising results.

## 1 Introduction

The *speaker identification* problem [11, 13, 27, 14] can be cast as a classification task aimed at determining if two voices were spoken by the same person or not. In this broad sense, it has applications in many fields. In particular, it is a crucial task in forensics, where there is a need to determine the speaker in phone calls. This application domain adds further complexity to the task. First, in illegal use of the phone the calls are typically anonymous and are short in duration. In addition, poor quality, ambient noise, interference, loss of signal (in the case of mobile phones), and reduced bandwidth may yield dramatic consequences. Traditionally, the problem has been tackled leveraging abilities of human experts in evaluating the similarities between voices, or in finding peculiarities and defects that allow one to identify the speaker. However, this practice has its drawbacks, among which the limited capabilities of humans in considering complex mixes of parameters and their subjectivity in evaluation.

Nowadays, the most popular methods for speaker identification are the following: (1) listening based methods [19]; (2) spectrograms comparison techniques [17, 10]; (3) phonetic parameters analysis [12, 1, 22, 29]; (4) automatic techniques [9, 8]. In particular, the latter represents a modern alternative to overcome the subjective evaluation of experts, since it relies on algorithmic procedures to predict whether two voices come from the same speaker or not. So, it may ensure more fairness to the classification procedure.

The need of fairness is one of the main motivations for which this research field is so primary for judiciary contexts. Forensics aims to be a fair scientific support to the logical composition of crime events. In this case, such support regards the phone-speaker identification.

From a technical point of view, we can distinguish between *closed* tests (aimed at finding the speaker in a set of voices that surely includes a sample of the speaker’s voice) and *open* tests (where this is not ensured). This paper deals with the open case, proposing a technique that uses the differences in speech of a set of different voices to build a population model, and the suspected person’s voice to build a speaker model, and then carries out the classification by evaluating the similarity among this models and the anonymous voice. While a preliminary evaluation of this approach was presented in [26], this work aims at a specific analysis of results with respect to the feature selection perspective.

The remainder of this work will present some related work and preprocessing details in Section 2, then our approach follows in Section 3, after that experimental evaluation is reported in Section 4. Finally, Section 5 will conclude with some considerations and future works.

## 2 Related works, Background and Preprocessing

Different features may describe the sounds produced by the human vocal apparatus, depending on how it is classified. A first classification is between consonants and vowels. Consonants are produced by forcing air passage in the restricted vocal apparatus. They can be further divided in voiceless, if produced without vibration of vocal cords, or voiced, otherwise. Vowels are produced when the apparatus puts no obstacles, and the sound is determined by the position of tongue and lips. Specifically, they are a periodic signal produced by three factors: the periodic movement of vocal cords that produces the *fundamental frequency* ( $f_0$  – related with the vocal tone of a person); the noise produced by the phonation; the modification of the sound caused by the sound expansion in the mouth. Such components make up the *frequency spectrum*. It is characterized by a sequence of peaks that change depending on the type of sound pronounced, a complex result of the cooperation of tongue, teeth, palate, lips, and so on. The frequency spectrum interacts with the the harmonic structure of speech (integer multiples of the fundamental frequency). The harmonics near to the resonance frequency are called *formants*.

A spectrogram is a plot that represents the components of the sound in three dimensions: time (on the  $x$  axis), frequency (on the  $y$  axis) and intensity

(represented using several intensities of gray). The inner values are usually represented in Hertz. The lower frequency is known as *first formant*  $f_1$ , followed by the successive peaks named  $f_2$ ,  $f_3$ , and so on. Generally, vowels are captured by  $f_1$  and  $f_2$ , since the first formant indicates the vertical tongue movement (i.e., up or down), and the second indicates the horizontal tongue movement (i.e., back or forth). Furthermore,  $f_2$  and  $f_3$  may provide useful hints for the lips rounding. Formant frequencies are widely accepted features for use in forensic phonetics [16]. Several works are based on the study of  $f_0$  only (e.g., [18]). Unfortunately, to date we cannot assert that voice is like a signature. So, in order to identify the speaker one needs as much information as possible, and it is questionable the fundamental frequency, alone, can be enough.

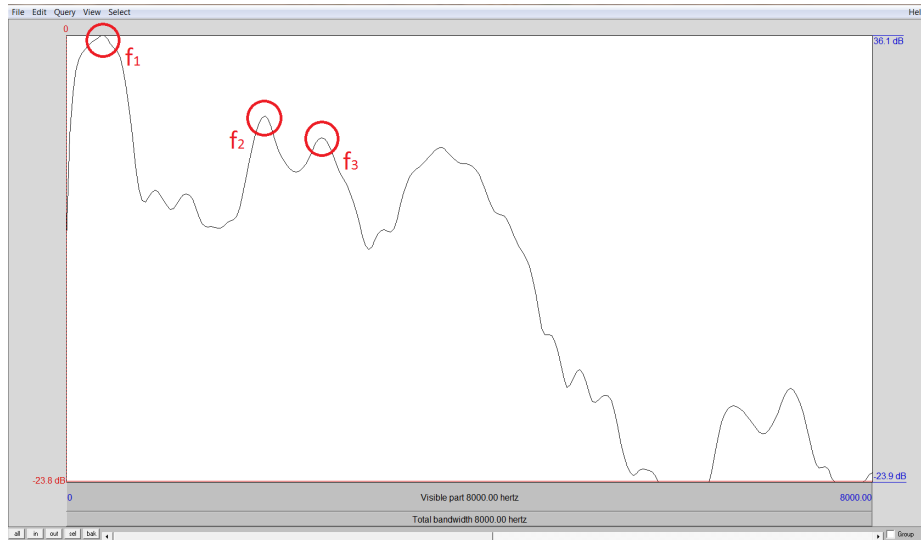
In order to overcome the uncertainty of the results using the fundamental frequency, [3] investigated the use of the first three formant frequencies and associated bandwidth. They are modeled using a multivariate Gaussian Mixture Model, in order to represent the vocal tract characteristics of the speaker, accounting for within-speaker variability. The results are expressed as a likelihood ratio, and highlight that since formants describe the cavity resonance, they are better suited for application in forensic speaker verification than Mel-Frequency Cepstral Coefficients (MFCC).

In [2], the authors focused on feature selection, investigating several ways to extract Cepstral Coefficients using the two major technologies for mobile communication (GSM and CDMA). Their approach uses the likelihood ratio to quantify the strength of speech evidence. The experiment highlighted the goodness of the MFCC, in spite of the outcomes obtained in [3]. They argue that such results are justified by the removal of the relevant information about the glottal shaping and lip radiation components due to the coding in mobile phone networks (both GSM and CDMA), that should make formant features useless.

In speaker verification task (i.e., the process of verifying the claimed identity of a speaker based on the speech signal), [20, 5] create speakers model by measuring the fundamental frequency and formant frequencies of vowels ( $a$ ,  $e$ ,  $i$ ,  $o$ ), and estimating their distributions via Gaussian kernel density estimator. The long-term formant distributions are plotted and examined, accepting or rejecting the speaker. However, the authors pointed out that other information can be extracted from the shape of distributions. Likelihood Ratio [21] is exploited, like in this work, to evaluate the results in [5].

Our approach is text-independent: we consider only a real-valued, limited, and continuous signal, i.e., a function that represents the trend of a given physical quantity (in our case, sound waves and their spectrum) over time. If a signal has period  $T$  (i.e.,  $x(t + T) = x(t)$ ), then the function is known when its trend in a range of length  $T$  is known. The inverse of  $T$  is the fundamental frequency  $F = \frac{1}{T}$ , measured in Hertz if time is expressed in seconds.

Conversely, formants are obtained from the signal-frequency spectrum. They are the resonance frequency measured where there is an energy peak in the sound produced by the reflection of absorption of the air passage in the vocal apparatus.



**Fig. 1.** Formants recognition using Praat.

The fundamental frequency and the first three formants are the features of our speaker model.

The preprocessing step is carried out by a human operator that considers, for each word, only emphasized vowels, that are less affected by co-articulation and have a more constant signal than others. According to the literature (e.g., [5]), vowel *U* is not considered in this study. The human operator uses *Praat*<sup>1</sup>, a software system able to show the graphical trend of the signal energy, allowing one to select the vowel to be analysed and to estimate the power spectrum. He select the fundamental frequency  $f_0$  using the *CEPSTRUM* method (the result of the Fourier transformation applied to the signal spectrum measured in Decibel), and the formants  $f_1$ ,  $f_2$  and  $f_3$  (i.e., the first three peaks of the frequency spectrum captured via Fast Fourier Transform). Subsequent formants cannot be detected, due to the poor signal quality.

Figure 1 shows the measurement of the formants of the first vowel *E* in the Italian word *gente* (this particular GUI reports peaks of the spectrum, then the fundamental frequency  $f_0$  is not reported in this Figure).

### 3 Statistical Method Applied to the Recognition of the Talker - SMART

Suppose we have a distance measure. Then, we can describe the (possibly) large variability of voices among several speakers, as well as the small variability of several dialogues of the same speaker. Such a variability can be represented

<sup>1</sup> [www.fon.hum.uva.nl/praat/](http://www.fon.hum.uva.nl/praat/)

estimating a distribution of the distances, making a model of the population diversities, together with a distribution of the diversities of the speech produced by a speaker in several contexts. Unfortunately, often there are not enough tracks of the same speaker to evaluate such distributions. So, a method to artificially populate a dataset related to the single speaker is needed. Bootstrap [23] re-samples the dataset randomly picking whole records and repeating them. It cannot do otherwise, since the formants are related by complex relationships that impose to keep them together [25].

**Missing data** Often the recordings have poor quality, making hard the detection of some formants. We need to manage missing data. In order to face this necessity we adopted some policies. If the fundamental frequency is missing, the average of the known values is assigned to this cell; if the third formant is missing, the cell is filled by its average conditioned by the values of the other formants, obtained via multiple regression; if the missing values are too many in a dimension, such dimension is removed completely, since estimations over few values are not reliable; finally, first and second formants hardly are lacking. However, it might happen that there are no values for a vowel. In such a case the subject is pulled out from the dataset.

**Speaker representation** Given a generic speaker  $k$ , a generic vowel will be represented as  $V_k \in \mathbb{R}^{N \times 4}$ , where  $N$  is the number of that vowel instances, whereas 4 stands for the fundamental frequency and the three formants. Considering that we measured only the instances of vowels  $A$ ,  $E$ ,  $I$  and  $O$ , we have  $V_{kj} \in \mathbb{R}^{N_{kj} \times 4}$  such that  $j \in \{A, E, I, O\}$ , and  $N_{kj}$  is the total amount of instances of the vowel  $j$ , speaker  $k$ . A speaker will be represented averaging the values over the columns, obtaining, for each  $V_{kj}$  a row vector  $\bar{V}_{kj}$ . Then:

$$\bar{S}_k = [\bar{V}_{kA}, \bar{V}_{kE}, \bar{V}_{kI}, \bar{V}_{kO}] \in \mathbb{R}^{1 \times 16}$$

where 16 is the total amount of vowels formants.

For the sake of completeness, we can give a fast look to an example of real data. Fixed the speaker  $k$  and the instance  $i_0$  of the vowel  $A$ , we have:

$$V_{kA}(i_0) = [f_{00}, f_{01}, f_{02}, f_{03}]$$

an example record of which might be:

$$V_{kA}(i_0) = [129, 635, 1288, 2325]$$

**Mahalanobis distance and Statistical distribution** Several measures have been investigated in [6, 7, 15, 24]. Summing up the results, these works shown the goodness of the Mahalanobis distance, that considers the position of the observations, it weights each observation with a coefficient extracted from the empirical covariance matrix. Such a matrix can be computed over the observed

values, it represents the relationship between the features and shows how much a feature changes if related to the other ones.

A covariance matrix  $\Sigma$  is computed over population matrix  $S$ , obtained chaining down the subjects in the population. In particular, recalling that each vowel of a speaker  $k$  is  $V_{kj} \in \mathbb{R}^{N_{kj} \times 4}$  with  $j \in \{A, E, I, O\}$ , we expect different values for each  $N_{kj}$ , from which we can compute:

$$M_k = \max_{j=\{A,E,I,O\}}(N_{kj})$$

The gap of each matrix that does not have  $M_k$  rows is filled. The instances are duplicated in the same order starting from the first, until the  $M_k$  number of rows is reached. The result, for each vowel, is a new matrix  $V'_{kj}$ . The representation of the speaker  $S_k$  will be:

$$S_k = [V'_{kA}, V'_{kE}, V'_{kI}, V'_{kO}] \in \mathbb{R}^{M_k \times 16}$$

where 16 is the total amount of vowels formants. We obtain  $S$  chaining down each  $S_k$ .

At this point, given two subjects represented as  $\bar{S}_i$  and  $\bar{S}_j$ , computed averaging column values of the respective matrices, the Mahalanobis distance  $d(\cdot, \cdot)$  is:

$$d(\bar{S}_i, \bar{S}_j) = \sqrt{(\bar{S}_i - \bar{S}_j) \Sigma^{-1} (\bar{S}_i - \bar{S}_j)^T}$$

Now, suppose we have a pair of voices and we want to evaluate the possibility that they are produced by the same speaker or not. From a Bayesian point of view, we can introduce two statistical hypotheses to encode these possibilities. Say  $H_0$  the *accusatory hypothesis*:

$$P(H_0|d) = \frac{P(H_0)P(d|H_0)}{nf}$$

and  $H_1$  the *defensive hypothesis*:

$$P(H_1|d) = \frac{P(H_1)P(d|H_1)}{nf}$$

where  $nf$  is a normalization factor. We can combine them, obtaining:

$$\frac{P(H_0|d)}{P(H_1|d)} = \frac{P(H_0) P(d|H_0) nf}{P(H_1) P(d|H_1) nf} = \left( \frac{P(H_0)}{P(H_1)} \right) \cdot lr(d)$$

$$lr(d) = \frac{P(d|H_0)}{P(d|H_1)} = \frac{p_B(d)}{p_W(d)}$$

where  $lr(d)$  denotes the likelihood ratio over  $d$ ,  $p_B(d)$  is the distribution of distance between the suspected speaker and the population (a.k.a. inter-distance), whereas  $p_W(d)$  is the distribution of distance taken within different instances of the suspected speaker (a.k.a. intra-distance). Note that  $p_B(d)$  and  $p_W(d)$  are real valued functions of  $d$ . The strength of evidence is computed in  $d(S_i, S_j)$  where

$S_i$  is the evidence speaker and  $S_j$  is the suspected speaker. Then, in our case,  $d$  is:

$$lr(d(S_i, S_j)) = \frac{P(d(S_i, S_j)|H_0)}{P(d(S_i, S_j)|H_1)} = \frac{p_B(d(S_i, S_j))}{p_W(d(S_i, S_j))}$$

Anyhow, the computation of  $p_W(d)$  is not so direct, since often the sample is poor (just a few minutes of recording for the suspected person’s voice). So, we need to refill the gap recurring to the bootstrap [23] procedure. It builds simulated registration using a random movement of the suspected person’s data, generating as many samples as the subjects of the population. For each sample the Mahalanobis distance is computed between it and the original one.

**Estimating speakers distributions** In order to estimate  $p_{B/W}(d)$  we exploit a semi-parametric kernel estimator method. Direct Plug-in Kernel [28] (as used in [7, 15]), needs to estimate its smoothing parameter  $h$ , using  $lsdpi(\cdot)$ , shown in Algorithm 1. The semi-parametric kernel [4] is:

$$\tilde{p}_{B/W}(d) = \frac{1}{N} \sum_{j=1}^N \frac{1}{h} H\left(\frac{d - d_j}{h}\right)$$

where  $\tilde{p}_{B/W}(d)$  denotes the model density of  $p_B$  or  $p_W$ ,  $N$  is the size of the population,  $d_j$  is the distance between  $S_k$  and  $S_j$ ,  $h$  is the smoothing parameter chosen via  $l$ -stage Direct Plug-in Kernel,  $H(\cdot)$  is the kernel function (Gaussian in our case).

Such parameters ensure the satisfaction of:

$$H(\cdot) \geq 0$$

and

$$\int H(\cdot) du = 1$$

in this way the first formula will satisfy  $\tilde{p}(d) \geq 0$  and  $\int \tilde{p}(d) dx = 1$ , as required for a function to be a probability density function.

## 4 Evaluation

We considered a dataset of Italian-male phone-call recordings, represented as described in Section 2 and made up as follows.  $K = \{k_1, \dots, k_i, \dots, k_m\}$  is the set of paired entry (in this experimental setting, we evaluated 50 positive entries).  $P$  is the set of single entries (they have not a paired recordings, so they can be used only as negative examples – in this experimental setting, we evaluated 350 single entries). So, we have just  $K$  positive test, while the number of negative tests will be:

$$nt(K, P) = \frac{P(P - 1)}{2} + 2KP + \left(4 \frac{K(K - 1)}{2}\right)$$

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**Algorithm 1**  $lsdpi(\cdot)$  –  $l$ -stage Direct Plug-in.

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**Input:** Number of stages  $l$ , kernel function  $K(\cdot)$  of order 2, a data sample  $X$ .**Output:** Approximation of  $\psi_c$ .
$$\hat{\sigma} \leftarrow \sqrt{Var(X)}$$
$$c \leftarrow r + 2l$$
$$\psi_c \leftarrow \frac{(-1)^{\frac{c}{2}} c!}{(2\hat{\sigma})^{c+1} (\frac{c}{2})! \sqrt{\pi}}$$
$$c \leftarrow c - 1$$
**while**  $c \geq 1$  **do**
$$g \leftarrow \left[ \frac{-2K^c 0}{\mu_2(K)\psi_{c+2} n} \right]^{\frac{1}{2c+5}}$$
$$\psi_c \leftarrow n^{-1} \sum_{i=1}^n \sum_{j=1}^n K_g^r(X_i - X_j)$$
$$c \leftarrow c - 2$$
**end while**  
return  $\psi_c$ 

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In this experimental setting,  $nt(50, 350) = 100.975$ . Our evaluation has a two-fold objective: on the one hand, understanding the performance, on the other, finding the set of formants that best represent a voice signature.

**Table 1.** Feature-subset performances

Tested features	EER	AUC
$f_0, f_1, f_2, f_3$	0.07692	0.98620
$f_1, f_2, f_3$	0.07692	0.98108
$f_0, f_2, f_3$	0.05406	<b>0.99295</b>
$f_0, f_1, f_3$	0.07658	0.98587
$f_0, f_1, f_2$	0.07182	0.98295
$f_0, f_1$	0.11538	0.96489
$f_0, f_2$	0.08800	0.97306
$f_0, f_3$	<b>0.03980</b>	0.98952
$f_1, f_2$	0.09615	0.97104
$f_1, f_3$	0.11022	0.96991
$f_2, f_3$	0.07692	0.97328

The Likelihood-Ratio  $lr(\cdot)$ , reported in Section 3, or its logarithm, expresses how many times more likely the data are under one model than the other. It has been used to build the graph in Figure 2, that shows which is the subset of features that maximizes the area under the ROC curve (AUC). Table 1 shows the Equal Error Rate (EER) and the Area Under the ROC Curve (AUC) for each subset. The former value is useful to balance the misclassification types, whereas the latter is used to identify the subset that makes less mistakes. The best EER in Table 1 is the curve nearest to zero in Figure 2, i.e. the subset



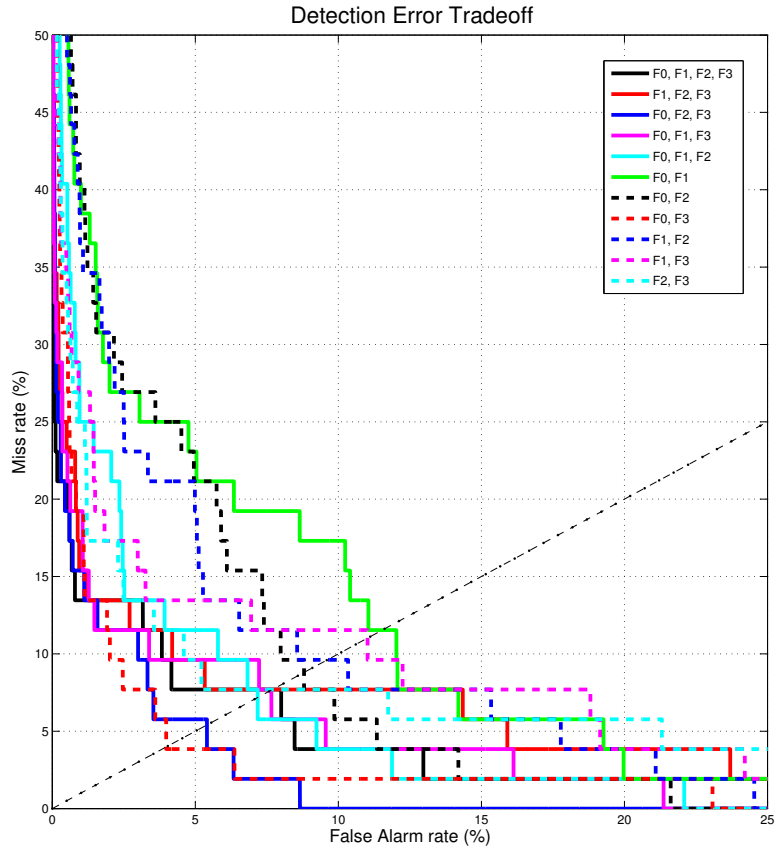


Fig. 2. Diagram of the feature-subset performances

$\{f_0, f_3\}$ , whereas the best AUC in Table 1 is the curve that goes faster to zero in both dimensions in Figure 2, i.e.  $\{f_0, f_2, f_3\}$ .

Since both include  $f_0$  and  $f_3$ , we should comment the role of  $f_2$ . Examining the subset  $\{f_0, f_2, f_3\}$  in Figure 2 we can see that the *false alarm rate* (the worst justice mistake) goes to zero faster than others. Looking at the values in Table 1, the EER of  $\{f_0, f_2, f_3\}$  is greater than the EER of  $\{f_0, f_3\}$  just a little bit with respect the trend of growth of the EER in general. Furthermore, the subset  $\{f_0, f_2, f_3\}$  gives the maximum value of AUC, denoting the smallest error area.

## 5 Conclusion

This work presented an approach to author identification that models the speaker via fundamental frequency and formant features. Distances among these descriptions have been computed using the Mahalanobis distance, in order to model the typical distance in speech among different speakers. Such a model has been obtained estimating the distributions of the differences. In particular, both the set of different speakers and the set of tracks recorded from the same speaker have been modeled, in order to obtain comparable models useful to decide if a novel speaker description is nearest to the unknown speaker model or it is nearest to the population model. Results seem to be relevant and comparable to other works.

Future works will be focused on clustering speaker description via unsupervised techniques, in order to understand whether formant features are enough to obtain clusters representing italian dialects.

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